Human Evolution and Economic Development

Oded Galor

October 8, 2019

Oded Galor

• Explores the coevolution of human traits & the growth process in the course of human history

- Explores the coevolution of human traits & the growth process in the course of human history
 - The effect of the growth process on:

- Explores the coevolution of human traits & the growth process in the course of human history
 - The effect of the growth process on:
 - The evolution in the composition of human traits

- Explores the coevolution of human traits & the growth process in the course of human history
 - The effect of the growth process on:
 - The evolution in the composition of human traits
 - The impact of the evolution in the composition of human traits on:

- Explores the coevolution of human traits & the growth process in the course of human history
 - The effect of the growth process on:
 - The evolution in the composition of human traits
 - The impact of the evolution in the composition of human traits on:
 - The growth process

• The coevolution of human traits and the growth process is critical for the understanding of the transition from stagnation to growth

- The coevolution of human traits and the growth process is critical for the understanding of the transition from stagnation to growth
- The Malthusian pressure affected

- The coevolution of human traits and the growth process is critical for the understanding of the transition from stagnation to growth
- The Malthusian pressure affected
 - The size of the population

- The coevolution of human traits and the growth process is critical for the understanding of the transition from stagnation to growth
- The Malthusian pressure affected
 - The size of the population
 - The composition of the population

- The coevolution of human traits and the growth process is critical for the understanding of the transition from stagnation to growth
- The Malthusian pressure affected
 - The size of the population
 - The composition of the population
- Hereditary (physical and cognitive) traits that were complementary to the growth process

- The coevolution of human traits and the growth process is critical for the understanding of the transition from stagnation to growth
- The Malthusian pressure affected
 - The size of the population
 - The composition of the population
- Hereditary (physical and cognitive) traits that were complementary to the growth process
 - Generated higher income

- The coevolution of human traits and the growth process is critical for the understanding of the transition from stagnation to growth
- The Malthusian pressure affected
 - The size of the population
 - The composition of the population
- Hereditary (physical and cognitive) traits that were complementary to the growth process
 - Generated higher income
 - Higher reproductive success

- The coevolution of human traits and the growth process is critical for the understanding of the transition from stagnation to growth
- The Malthusian pressure affected
 - The size of the population
 - The composition of the population
- Hereditary (physical and cognitive) traits that were complementary to the growth process
 - Generated higher income
 - Higher reproductive success
 - Became more prevalent in the population

- The coevolution of human traits and the growth process is critical for the understanding of the transition from stagnation to growth
- The Malthusian pressure affected
 - The size of the population
 - The composition of the population
- Hereditary (physical and cognitive) traits that were complementary to the growth process
 - Generated higher income
 - Higher reproductive success
 - Became more prevalent in the population
- Evolutionary processes (cultural or biological)

- The coevolution of human traits and the growth process is critical for the understanding of the transition from stagnation to growth
- The Malthusian pressure affected
 - The size of the population
 - The composition of the population
- Hereditary (physical and cognitive) traits that were complementary to the growth process
 - Generated higher income
 - Higher reproductive success
 - Became more prevalent in the population
- Evolutionary processes (cultural or biological)
 - Raised the prevalence of complementary traits to the growth process

- The coevolution of human traits and the growth process is critical for the understanding of the transition from stagnation to growth
- The Malthusian pressure affected
 - The size of the population
 - The composition of the population
- Hereditary (physical and cognitive) traits that were complementary to the growth process
 - Generated higher income
 - Higher reproductive success
 - Became more prevalent in the population
- Evolutionary processes (cultural or biological)
 - Raised the prevalence of complementary traits to the growth process
 - Reinforced the growth process

- The coevolution of human traits and the growth process is critical for the understanding of the transition from stagnation to growth
- The Malthusian pressure affected
 - The size of the population
 - The composition of the population
- Hereditary (physical and cognitive) traits that were complementary to the growth process
 - Generated higher income
 - Higher reproductive success
 - Became more prevalent in the population
- Evolutionary processes (cultural or biological)
 - Raised the prevalence of complementary traits to the growth process
 - Reinforced the growth process
 - Stimulated the take-off from stagnation to growth

Charles Darwin



1.0.1.0	00	ot:	0.0	
	~~~			

# The Critical Impact of Malthus on Darwin

 "In October 1838, that is, fifteen months after I had begun my systematic inquiry, I happened to read for amusement Malthus on Population, and being well prepared to appreciate the struggle for existence from long-continued observation of the habits of animals and plants, it at once struck me that under these circumstances favorable variations would tend to be preserved, and unfavorable ones to be destroyed." Charles Darwin

Intr	od.	ucti	ion.
	oui	acti	

# The Critical Impact of Malthus on Darwin

- "In October 1838, that is, fifteen months after I had begun my systematic inquiry, I happened to read for amusement Malthus on Population, and being well prepared to appreciate the struggle for existence from long-continued observation of the habits of animals and plants, it at once struck me that under these circumstances favorable variations would tend to be preserved, and unfavorable ones to be destroyed." Charles Darwin
  - Darwin: Favorable traits will be selected

Intr	od.	ucti	ion.
	oui	acti	

# The Critical Impact of Malthus on Darwin

- "In October 1838, that is, fifteen months after I had begun my systematic inquiry, I happened to read for amusement Malthus on Population, and being well prepared to appreciate the struggle for existence from long-continued observation of the habits of animals and plants, it at once struck me that under these circumstances favorable variations would tend to be preserved, and unfavorable ones to be destroyed." Charles Darwin
  - Darwin: Favorable traits will be selected
  - Galor-Moav: Among humans, complementary traits to the technological environment will be selected and they will contribute to technological change & the transition from stagnation to growth

## Evolution of the Human Brain - Relative Volume & Size of Cerebral Cortex



October 8, 2019 6 / 75

- At first glance
  - May appear as a trivial question:

- May appear as a trivial question:
  - Human brains permitted a standard of living that no other species has ever achieved

- May appear as a trivial question:
  - Human brains permitted a standard of living that no other species has ever achieved
- Deeper reflections

- May appear as a trivial question:
  - Human brains permitted a standard of living that no other species has ever achieved
- Deeper reflections
  - If the brain is indeed so beneficial for reproductive success, why only humans developed such a brain over billions of years of evolution?

- May appear as a trivial question:
  - Human brains permitted a standard of living that no other species has ever achieved
- Deeper reflections
  - If the brain is indeed so beneficial for reproductive success, why only humans developed such a brain over billions of years of evolution?
  - Rare random event? NO

- May appear as a trivial question:
  - Human brains permitted a standard of living that no other species has ever achieved
- Deeper reflections
  - If the brain is indeed so beneficial for reproductive success, why only humans developed such a brain over billions of years of evolution?
  - Rare random event? NO
    - Convergent Evolution: vitals organs evolved in parallel path across species (i.e., eyes)

• Disadvantageous:

- Disadvantageous:
  - Huge energy consumption

- Disadvantageous:
  - Huge energy consumption
    - 2% of the body mass & 20% of the body's energy consumption

- Disadvantageous:
  - Huge energy consumption
    - 2% of the body mass & 20% of the body's energy consumption
  - Large volume

- Disadvantageous:
  - Huge energy consumption
    - 2% of the body mass & 20% of the body's energy consumption
  - Large volume
    - Newborns have difficulty to pass through the birth canal

- Disadvantageous:
  - Huge energy consumption
    - 2% of the body mass & 20% of the body's energy consumption
  - Large volume
    - Newborns have difficulty to pass through the birth canal
    - $\bullet \ \Rightarrow$  Baby's brain is "half-baked" & babies are entirely vulnerable
# Trade-off Associated with the Human Brain

### Disadvantageous:

- Huge energy consumption
  - 2% of the body mass & 20% of the body's energy consumption
- Large volume
  - Newborns have difficulty to pass through the birth canal
  - $\bullet \ \Rightarrow$  Baby's brain is "half-baked" & babies are entirely vulnerable
  - $\bullet \ \Rightarrow$  Human are able to sustain themselves only in adolescence

# Trade-off Associated with the Human Brain

- Disadvantageous:
  - Huge energy consumption
    - 2% of the body mass & 20% of the body's energy consumption
  - Large volume
    - Newborns have difficulty to pass through the birth canal
    - $\bullet \ \Rightarrow$  Baby's brain is "half-baked" & babies are entirely vulnerable
    - $\bullet \ \Rightarrow$  Human are able to sustain themselves only in adolescence
- Advantageous (ex-post)

# Trade-off Associated with the Human Brain

### Disadvantageous:

- Huge energy consumption
  - 2% of the body mass & 20% of the body's energy consumption
- Large volume
  - Newborns have difficulty to pass through the birth canal
  - $\bullet \ \Rightarrow$  Baby's brain is "half-baked" & babies are entirely vulnerable
  - $\bullet\,\,\Rightarrow\,\,$  Human are able to sustain themselves only in adolescence
- Advantageous (ex-post)
  - Ability to conquer the environment & to become the masters of Earth

- The Ecological Hypothesis
  - The human brain evolved in reaction to environmental changes

- The human brain evolved in reaction to environmental changes
  - Fostered the developments of hunting-gathering strategies

- The human brain evolved in reaction to environmental changes
  - Fostered the developments of hunting-gathering strategies
  - Enabled the mapping of food sources

- The human brain evolved in reaction to environmental changes
  - Fostered the developments of hunting-gathering strategies
  - Enabled the mapping of food sources
- The Social hypothesis

- The human brain evolved in reaction to environmental changes
  - Fostered the developments of hunting-gathering strategies
  - Enabled the mapping of food sources
- The Social hypothesis
  - The human brain evolved to facilitate interaction across individuals: cooperation, competition & trade

- The human brain evolved in reaction to environmental changes
  - Fostered the developments of hunting-gathering strategies
  - Enabled the mapping of food sources
- The Social hypothesis
  - The human brain evolved to facilitate interaction across individuals: cooperation, competition & trade
    - Enabled the understanding of action & reaction of others

- The human brain evolved in reaction to environmental changes
  - Fostered the developments of hunting-gathering strategies
  - Enabled the mapping of food sources
- The Social hypothesis
  - The human brain evolved to facilitate interaction across individuals: cooperation, competition & trade
    - Enabled the understanding of action & reaction of others
    - Improved social standing via: persuasion & complements & lies & humor

- The Cultural Hypothesis
  - The human brain evolved to permit the learning of the experience accumulated by others over the generations

- The Cultural Hypothesis
  - The human brain evolved to permit the learning of the experience accumulated by others over the generations
    - Assimilate manners & customs that increased survival probability

- The Cultural Hypothesis
  - The human brain evolved to permit the learning of the experience accumulated by others over the generations
    - Assimilate manners & customs that increased survival probability
    - Permit cultural evolution as a substitute for biological adaptation

- The human brain evolved to permit the learning of the experience accumulated by others over the generations
  - Assimilate manners & customs that increased survival probability
  - Permit cultural evolution as a substitute for biological adaptation
- Sexual Selection

- The human brain evolved to permit the learning of the experience accumulated by others over the generations
  - Assimilate manners & customs that increased survival probability
  - Permit cultural evolution as a substitute for biological adaptation
- Sexual Selection
  - Humans develop a preference for partners with more developed brains

- The human brain evolved to permit the learning of the experience accumulated by others over the generations
  - Assimilate manners & customs that increased survival probability
  - Permit cultural evolution as a substitute for biological adaptation
- Sexual Selection
  - Humans develop a preference for partners with more developed brains
    - Inferring from the thought process about the qualities of the potential partner that may be important for the survival of their offspring

## Out of Africa - Homo Erectus



#### Evolution and Growth

## Out of Africa - Homo Erectus



#### Evolution and Growth

## Out of Africa - Homo Erectus



Oded Galor

#### Evolution and Growth

### Out of Africa - Homo sapiens



- Archeological Evidence
  - Nahal Me'arot The Carmel Mountain Range

- Nahal Me'arot The Carmel Mountain Range
  - On the migratory route out of Africa

- Nahal Me'arot The Carmel Mountain Range
  - On the migratory route out of Africa
  - 500,000 years of nearly continuous human existence

- Nahal Me'arot The Carmel Mountain Range
  - On the migratory route out of Africa
  - 500,000 years of nearly continuous human existence
  - Coexistence of Homo sapiens & Neanderthal

- Nahal Me'arot The Carmel Mountain Range
  - On the migratory route out of Africa
  - 500,000 years of nearly continuous human existence
  - Coexistence of Homo sapiens & Neanderthal
- Attractive location for humans

- Nahal Me'arot The Carmel Mountain Range
  - On the migratory route out of Africa
  - 500,000 years of nearly continuous human existence
  - Coexistence of Homo sapiens & Neanderthal
- Attractive location for humans
  - Ecological diversity

- Nahal Me'arot The Carmel Mountain Range
  - On the migratory route out of Africa
  - 500,000 years of nearly continuous human existence
  - Coexistence of Homo sapiens & Neanderthal
- Attractive location for humans
  - Ecological diversity
  - Scope for Hunting: Deer, Wild Goats & Bulls, Camels, Rhinoceros

- Nahal Me'arot The Carmel Mountain Range
  - On the migratory route out of Africa
  - 500,000 years of nearly continuous human existence
  - Coexistence of Homo sapiens & Neanderthal
- Attractive location for humans
  - Ecological diversity
  - Scope for Hunting: Deer, Wild Goats & Bulls, Camels, Rhinoceros
  - Scope for Gathering: Wild Wheat & Barley, Berries, Fruit Trees

- Nahal Me'arot The Carmel Mountain Range
  - On the migratory route out of Africa
  - 500,000 years of nearly continuous human existence
  - Coexistence of Homo sapiens & Neanderthal
- Attractive location for humans
  - Ecological diversity
  - Scope for Hunting: Deer, Wild Goats & Bulls, Camels, Rhinoceros
  - Scope for Gathering: Wild Wheat & Barley, Berries, Fruit Trees
  - Existence of raw material: Stone & Wood

- Nahal Me'arot The Carmel Mountain Range
  - On the migratory route out of Africa
  - 500,000 years of nearly continuous human existence
  - Coexistence of Homo sapiens & Neanderthal
- Attractive location for humans
  - Ecological diversity
  - Scope for Hunting: Deer, Wild Goats & Bulls, Camels, Rhinoceros
  - Scope for Gathering: Wild Wheat & Barley, Berries, Fruit Trees
  - Existence of raw material: Stone & Wood
  - Water sources

- Nahal Me'arot The Carmel Mountain Range
  - On the migratory route out of Africa
  - 500,000 years of nearly continuous human existence
  - Coexistence of Homo sapiens & Neanderthal
- Attractive location for humans
  - Ecological diversity
  - Scope for Hunting: Deer, Wild Goats & Bulls, Camels, Rhinoceros
  - Scope for Gathering: Wild Wheat & Barley, Berries, Fruit Trees
  - Existence of raw material: Stone & Wood
  - Water sources
  - Moderate Mediterranean climate

# Nahal Me'arot - The Carmel Mountain Range



## Nahal Me'arot - The Carmel Mountain Range










#### Nahal Me'arot - Tabun Cave



Oded Galor

#### Nahal Me'arot - Gamal Cave



#### Nahal Me'arot - Animals



Evolution - Human Brain

Archaeological Evidence

#### Nahal Me'arot - Water Source



#### Archaeological Evidence

#### Nahal Me'arot - Flint Tools



#### Nahal Me'arot - Stone Tools



#### Nahal Me'arot - Stone Tools



#### Oldest Bear Brewery - The Carmel Mountain Range

10/3/2019

13,000-year-old brewery discovered in Israel, the oldest in the world | The Times of Israel

FIND PREDATES GRAIN CEREAL DOMESTICATION BY 4,000 YEARS

### 13,000-year-old brewery discovered in Israel, the oldest in the world

Ancient Natufians tamed seven species of wild grains for ancient ale, according to new Stanford University study

Ry AMANDA BORSCHEL-DAN



12345

Which came first: beer or bread production? The 60-year-old archaeological debate is coming to a (frothy) head as a new Stanford University study of three 15,000-year-old stone mortars offers the earliest known physical evidence of an extensive ancient beer-brewing operation.

An international team of scientists discovered and tested residue from the motrars, which were used by the seminomatic Naturians and discovered not a graveyral atta called the Ragedre Cave, in the Carrow Holkontains near Halfa, Israel, according to a Standord News article on the discovery. The Naturians lived in the Levant between the Paleolithic and the Noolithic periods.

The find comes on the heels of a July report that archaeologists working in northeastern Jordan discovered the charred remains of bread baked by Naturfians some 11,600 to 14,600 years ago. According to the Stanford scientists, the ancient beer residue comes from 11,700 to 15,700 years old, potentially predating the bread.

Regardless of which came first, both the brewery and the bread production precede evidence of domesticated cereals in the Levant, which arrived some 4,000 years later.

Evolution and Growth

• Slow but steady technological progress

- Slow but steady technological progress
  - Use of fire

- Slow but steady technological progress
  - Use of fire
  - Progressive development of flint tools

- Slow but steady technological progress
  - Use of fire
  - Progressive development of flint tools
  - Progressive development of art & crafts

- Slow but steady technological progress
  - Use of fire
  - Progressive development of flint tools
  - Progressive development of art & crafts
- Steady evolution of the volume of the human brain

• Technological Change:

- Technological Change:
  - Use of fire for cooking

- Technological Change:
  - Use of fire for cooking
    - Consumption of cooked food

- Technological Change:
  - Use of fire for cooking
    - Consumption of cooked food
    - Reduction in energy & muscles needed for chewing & digestion

- Technological Change:
  - Use of fire for cooking
    - Consumption of cooked food
    - Reduction in energy & muscles needed for chewing & digestion
- Evolution of the human brain

- Technological Change:
  - Use of fire for cooking
    - Consumption of cooked food
    - Reduction in energy & muscles needed for chewing & digestion
- Evolution of the human brain
  - Brain size increased

- Technological Change:
  - Use of fire for cooking
    - Consumption of cooked food
    - $\bullet\,$  Reduction in energy & muscles needed for chewing & digestion
- Evolution of the human brain
  - Brain size increased
    - Diversion of energy from chewing & digesting to brain maintenance

- Technological Change:
  - Use of fire for cooking
    - Consumption of cooked food
    - Reduction in energy & muscles needed for chewing & digestion
- Evolution of the human brain
  - Brain size increased
    - Diversion of energy from chewing & digesting to brain maintenance
    - Enlarging the brain on the account of the jaw and its muscles

• Technological change:

- Technological change:
  - Development of wooden spears & sharp stones

- Technological change:
  - Development of wooden spears & sharp stones
- Evolution of human traits

- Technological change:
  - Development of wooden spears & sharp stones
- Evolution of human traits
  - Selection of good throwers

- Technological change:
  - Development of wooden spears & sharp stones
- Evolution of human traits
  - Selection of good throwers
- Further technological Change:

- Technological change:
  - Development of wooden spears & sharp stones
- Evolution of human traits
  - Selection of good throwers
- Further technological Change:
  - Development of better spears & bow and arrow

- Technological change:
  - Development of wooden spears & sharp stones
- Evolution of human traits
  - Selection of good throwers
- Further technological Change:
  - Development of better spears & bow and arrow
- ...Further evolution of human traits...

• Evolutionary advantage of predisposition toward investment in human capital in the Malthusian epoch due to:

- Evolutionary advantage of predisposition toward investment in human capital in the Malthusian epoch due to:
  - The evolution of the human brain complemented investment in human capital

- Evolutionary advantage of predisposition toward investment in human capital in the Malthusian epoch due to:
  - The evolution of the human brain complemented investment in human capital
  - Increased economic complexity in the course of the Neolithic Revolution

- Evolutionary advantage of predisposition toward investment in human capital in the Malthusian epoch due to:
  - The evolution of the human brain complemented investment in human capital
  - Increased economic complexity in the course of the Neolithic Revolution
- The Malthusian pressure
- Evolutionary advantage of predisposition toward investment in human capital in the Malthusian epoch due to:
  - The evolution of the human brain complemented investment in human capital
  - Increased economic complexity in the course of the Neolithic Revolution
- The Malthusian pressure
  - Raised the evolutionary advantage of traits associated with predisposition towards investment in human capital:

- Evolutionary advantage of predisposition toward investment in human capital in the Malthusian epoch due to:
  - The evolution of the human brain complemented investment in human capital
  - Increased economic complexity in the course of the Neolithic Revolution
- The Malthusian pressure
  - Raised the evolutionary advantage of traits associated with predisposition towards investment in human capital:
    - Preference for child quality (Galor-Moav (QJE 2002)

- Evolutionary advantage of predisposition toward investment in human capital in the Malthusian epoch due to:
  - The evolution of the human brain complemented investment in human capital
  - Increased economic complexity in the course of the Neolithic Revolution
- The Malthusian pressure
  - Raised the evolutionary advantage of traits associated with predisposition towards investment in human capital:
    - Preference for child quality (Galor-Moav (QJE 2002)
    - Higher life expectancy (Galor-Moav, 2005, 2007)

- Evolutionary advantage of predisposition toward investment in human capital in the Malthusian epoch due to:
  - The evolution of the human brain complemented investment in human capital
  - Increased economic complexity in the course of the Neolithic Revolution
- The Malthusian pressure
  - Raised the evolutionary advantage of traits associated with predisposition towards investment in human capital:
    - Preference for child quality (Galor-Moav (QJE 2002)
    - Higher life expectancy (Galor-Moav, 2005, 2007)
    - Entrepreneurial spirit (Galor-Michalopoulos, JET 2012)

- Evolutionary advantage of predisposition toward investment in human capital in the Malthusian epoch due to:
  - The evolution of the human brain complemented investment in human capital
  - Increased economic complexity in the course of the Neolithic Revolution
- The Malthusian pressure
  - Raised the evolutionary advantage of traits associated with predisposition towards investment in human capital:
    - Preference for child quality (Galor-Moav (QJE 2002)
    - Higher life expectancy (Galor-Moav, 2005, 2007)
    - Entrepreneurial spirit (Galor-Michalopoulos, JET 2012)
    - Moderate fecundity (Galor-Klemp, Nature E&E 2019)

- Evolutionary advantage of predisposition toward investment in human capital in the Malthusian epoch due to:
  - The evolution of the human brain complemented investment in human capital
  - Increased economic complexity in the course of the Neolithic Revolution
- The Malthusian pressure
  - Raised the evolutionary advantage of traits associated with predisposition towards investment in human capital:
    - Preference for child quality (Galor-Moav (QJE 2002)
    - Higher life expectancy (Galor-Moav, 2005, 2007)
    - Entrepreneurial spirit (Galor-Michalopoulos, JET 2012)
    - Moderate fecundity (Galor-Klemp, Nature E&E 2019)
    - Time preference (Galor-Ozak (AER 2016)

- Evolutionary advantage of predisposition toward investment in human capital in the Malthusian epoch due to:
  - The evolution of the human brain complemented investment in human capital
  - Increased economic complexity in the course of the Neolithic Revolution
- The Malthusian pressure
  - Raised the evolutionary advantage of traits associated with predisposition towards investment in human capital:
    - Preference for child quality (Galor-Moav (QJE 2002)
    - Higher life expectancy (Galor-Moav, 2005, 2007)
    - Entrepreneurial spirit (Galor-Michalopoulos, JET 2012)
    - Moderate fecundity (Galor-Klemp, Nature E&E 2019)
    - Time preference (Galor-Ozak (AER 2016)
    - Loss Aversion (Galor-Savitskiy, 2019)

• Evolution of new traits may be a slow process

- Evolution of new traits may be a slow process
  - Human eye: evolved over 540 millions of years

- Evolution of new traits may be a slow process
  - Human eye: evolved over 540 millions of years
- Rapid evolution in the composition of traits in a population

- Evolution of new traits may be a slow process
  - Human eye: evolved over 540 millions of years
- Rapid evolution in the composition of traits in a population
  - Evolution of the English Peppered Moth

- Evolution of new traits may be a slow process
  - Human eye: evolved over 540 millions of years
- Rapid evolution in the composition of traits in a population
  - Evolution of the English Peppered Moth
    - Triggered by industrial pollution (few hundreds generations)

- Evolution of new traits may be a slow process
  - Human eye: evolved over 540 millions of years
- Rapid evolution in the composition of traits in a population
  - Evolution of the English Peppered Moth
    - Triggered by industrial pollution (few hundreds generations)
  - Evolution of Darwin's Finches

- Evolution of new traits may be a slow process
  - Human eye: evolved over 540 millions of years
- Rapid evolution in the composition of traits in a population
  - Evolution of the English Peppered Moth
    - Triggered by industrial pollution (few hundreds generations)
  - Evolution of Darwin's Finches
    - Triggered by drought in the Galápagos (few generations)

- Evolution of new traits may be a slow process
  - Human eye: evolved over 540 millions of years
- Rapid evolution in the composition of traits in a population
  - Evolution of the English Peppered Moth
    - Triggered by industrial pollution (few hundreds generations)
  - Evolution of Darwin's Finches
    - Triggered by drought in the Galápagos (few generations)
  - Evolution of guppies's decoration

- Evolution of new traits may be a slow process
  - Human eye: evolved over 540 millions of years
- Rapid evolution in the composition of traits in a population
  - Evolution of the English Peppered Moth
    - Triggered by industrial pollution (few hundreds generations)
  - Evolution of Darwin's Finches
    - Triggered by drought in the Galápagos (few generations)
  - Evolution of guppies's decoration
    - Triggered by the introduction of new predators (15 generations)

- Evolution of new traits may be a slow process
  - Human eye: evolved over 540 millions of years
- Rapid evolution in the composition of traits in a population
  - Evolution of the English Peppered Moth
    - Triggered by industrial pollution (few hundreds generations)
  - Evolution of Darwin's Finches
    - Triggered by drought in the Galápagos (few generations)
  - Evolution of guppies's decoration
    - Triggered by the introduction of new predators (15 generations)
    - Trade-off: attracting sexual mates & predators

# Rapid Evolution of the English Peppered Moth



# • Severe drought in the Daphne Major Island (Galápagos)

- Severe drought in the Daphne Major Island (Galápagos)
  - Increased in size & hardness of seeds

- Severe drought in the Daphne Major Island (Galápagos)
  - Increased in size & hardness of seeds
    - Competition over scarce seeds

- Severe drought in the Daphne Major Island (Galápagos)
  - Increased in size & hardness of seeds
    - Competition over scarce seeds
  - Triggered diverging beak sizes (character displacment)

- Severe drought in the Daphne Major Island (Galápagos)
  - Increased in size & hardness of seeds
    - Competition over scarce seeds
  - Triggered diverging beak sizes (character displacment)
    - Smaller beaks among the medium finch (Geospiza fortis)

- Severe drought in the Daphne Major Island (Galápagos)
  - Increased in size & hardness of seeds
    - Competition over scarce seeds
  - Triggered diverging beak sizes (character displacment)
    - Smaller beaks among the medium finch (Geospiza fortis)
    - Larger beaks among large ground finch (Geospiza magnirostris)

- Severe drought in the Daphne Major Island (Galápagos)
  - Increased in size & hardness of seeds
    - Competition over scarce seeds
  - Triggered diverging beak sizes (character displacment)
    - Smaller beaks among the medium finch (Geospiza fortis)
    - Larger beaks among large ground finch (Geospiza magnirostris)
  - Higher representation of large finches

- Severe drought in the Daphne Major Island (Galápagos)
  - Increased in size & hardness of seeds
    - Competition over scarce seeds
  - Triggered diverging beak sizes (character displacment)
    - Smaller beaks among the medium finch (Geospiza fortis)
    - Larger beaks among large ground finch (Geospiza magnirostris)
  - Higher representation of large finches
    - Enhanced partly by sexual selection



#### Archaeological Evidence

# Rapid Evolution in Guppies



• Lactose Tolerance

- Lactose Tolerance
  - Variations in the ability to tolerate lactose across regions

- Lactose Tolerance
  - Variations in the ability to tolerate lactose across regions
    - Governed by the timing of the transition to agriculture & domestication of dairy animals

- Lactose Tolerance
  - Variations in the ability to tolerate lactose across regions
    - Governed by the timing of the transition to agriculture & domestication of dairy animals
- Genetic immunity to malaria Sickle Cell Trait

- Lactose Tolerance
  - Variations in the ability to tolerate lactose across regions
    - Governed by the timing of the transition to agriculture & domestication of dairy animals
- Genetic immunity to malaria Sickle Cell Trait
  - Variations in natural immunity to malaria

- Lactose Tolerance
  - Variations in the ability to tolerate lactose across regions
    - Governed by the timing of the transition to agriculture & domestication of dairy animals
- Genetic immunity to malaria Sickle Cell Trait
  - Variations in natural immunity to malaria
    - Triggered by engagement in slash-and-burn agriculture

- Lactose Tolerance
  - Variations in the ability to tolerate lactose across regions
    - Governed by the timing of the transition to agriculture & domestication of dairy animals
- Genetic immunity to malaria Sickle Cell Trait
  - Variations in natural immunity to malaria
    - Triggered by engagement in slash-and-burn agriculture
- 700 regions of the human genome

- Lactose Tolerance
  - Variations in the ability to tolerate lactose across regions
    - Governed by the timing of the transition to agriculture & domestication of dairy animals
- Genetic immunity to malaria Sickle Cell Trait
  - Variations in natural immunity to malaria
    - Triggered by engagement in slash-and-burn agriculture
- 700 regions of the human genome
  - Reshaped by natural selection in the past 5,000-15,000 years (Voight et al., 2006)
### Evolutionary Changes in Humans in the Past 10,000 Years

- Lactose Tolerance
  - Variations in the ability to tolerate lactose across regions
    - Governed by the timing of the transition to agriculture & domestication of dairy animals
- Genetic immunity to malaria Sickle Cell Trait
  - Variations in natural immunity to malaria
    - Triggered by engagement in slash-and-burn agriculture
- 700 regions of the human genome
  - Reshaped by natural selection in the past 5,000-15,000 years (Voight et al., 2006)
- Genetic loci associated with immunity, pigmentation, and height

# Evolutionary Changes in Humans in the Past 10,000 Years

- Lactose Tolerance
  - Variations in the ability to tolerate lactose across regions
    - Governed by the timing of the transition to agriculture & domestication of dairy animals
- Genetic immunity to malaria Sickle Cell Trait
  - Variations in natural immunity to malaria
    - Triggered by engagement in slash-and-burn agriculture
- 700 regions of the human genome
  - Reshaped by natural selection in the past 5,000-15,000 years (Voight et al., 2006)
- Genetic loci associated with immunity, pigmentation, and height
  - Strong positive selection since the Neolithic transition (Mathieson et al., 2015)

### The Benchmark Model – Galor-Moav (QJE 2002)

• Overlapping-generations economy

### The Benchmark Model – Galor-Moav (QJE 2002)

- Overlapping-generations economy
- t = 0, 1, 2, 3...

### The Benchmark Model – Galor-Moav (QJE 2002)

- Overlapping-generations economy
- t = 0, 1, 2, 3...
- One homogeneous good

## The Benchmark Model – Galor-Moav (QJE 2002)

- Overlapping-generations economy
- *t* = 0, 1, 2, 3...
- One homogeneous good
- 2 factors of production:
  - Labor (measured in efficiency units)
  - Land

# Factor Supply

- Land is fixed over time
  - Surface of planet earth

## Factor Supply

- Land is fixed over time
  - Surface of planet earth
- Efficiency units of labor evolves endogenously
  - Determined by households' decisions about the number and level of human capital of their children

Theory	The Main Elements
Main Elements	

Т	heory	

- The Malthusian Structure
- The Darwinian Structure

Т	heorv	

- The Malthusian Structure
- The Darwinian Structure
- Sources of Technological Progress

_		
	hoong	
	neurv	

- The Malthusian Structure
- The Darwinian Structure
- Sources of Technological Progress
- Origins of Human Capital Formation

_		
	hoone	
	neurv	

- The Malthusian Structure
- The Darwinian Structure
- Sources of Technological Progress
- Origins of Human Capital Formation
- Triggers of the Demographic Transition

_	
	boond
	neorv

• A subsistence consumption constraint

heory	

- A subsistence consumption constraint
- Positive effect of income on population

• 
$$y \uparrow \Longrightarrow L \uparrow$$

heory	

- A subsistence consumption constraint
- Positive effect of income on population

•  $y \uparrow \Longrightarrow L \uparrow$ 

• Fixed factor of production - Land

• 
$$L \uparrow \Longrightarrow AP_L \downarrow \Longrightarrow y \downarrow$$

т	hoom	
	neory	

- A subsistence consumption constraint
- Positive effect of income on population

•  $y \uparrow \Longrightarrow L \uparrow$ 

- Fixed factor of production Land
  - $L \uparrow \Longrightarrow AP_L \downarrow \Longrightarrow y \downarrow$
- Output per capita fluctuates (with a negligible trend) around a constant level in the long-run
  - Reflecting diminishing returns to labor & positive effect of income on population

Theory	The Main Elements
Production	

• The output produced in period t

$$Y_t = H_t^{1-\alpha} (A_t X)^{\alpha}$$

- $H_t \equiv$  efficiency units of labor
- $A_t \equiv$  technological level
- $X \equiv \text{land}$

Theory	The Main E
Production	

• The output produced in period t

$$Y_t = H_t^{1-\alpha} (A_t X)^{\alpha}$$

lements

• 
$$H_t \equiv$$
 efficiency units of labor

• 
$$A_t \equiv$$
 technological level

• 
$$X \equiv \text{land}$$

• Output per efficiency units of labor at time t

$$y_t = x_t^{\alpha}$$

•  $x_t \equiv (A_t X)/H_t \equiv$  effective resources per worker

## The Malthusian Structure – Effects of Technological Progress

• Very short-run (for a given population):

•  $A_t \uparrow \implies y_t \uparrow (above \bar{y})$ 

# The Malthusian Structure – Effects of Technological Progress

• Very short-run (for a given population):

• 
$$A_t \uparrow \implies y_t \uparrow (above \bar{y})$$

• Short-run (initial adjustment of population):

• 
$$y_t \uparrow \implies L_t \uparrow$$

# The Malthusian Structure – Effects of Technological Progress

• Very short-run (for a given population):

• 
$$A_t \uparrow \implies y_t \uparrow (above \bar{y})$$

• Short-run (initial adjustment of population):

• 
$$y_t \uparrow \implies L_t \uparrow$$

• Long-run (population reaches a new steady-state):

• 
$$L_t \uparrow \Longrightarrow y \downarrow (\text{back to } \bar{y})$$

Т	h	e	0	n	1	

## Sources of Technological Progress

• Average individuals' quality affects technological progress

$$e_t \uparrow \implies A_t \uparrow$$

# Sources of Technological Progress

• Average individuals' quality affects technological progress

$$e_t \uparrow \implies A_t \uparrow$$

• human capital provides an advantage in adopting and advancing new technologies

#### The Main Elements

# Technological Progress

$$g_{t+1} \equiv \frac{A_{t+1} - A_t}{A_t} = \psi(e_t)$$

• 
$$g_{t+1} \equiv$$
 rate of tech progress

•  $e_t \equiv$  average quality

#### The Main Elements

# **Technological Progress**

$$g_{t+1} \equiv \frac{A_{t+1} - A_t}{A_t} = \psi(e_t)$$

• 
$$g_{t+1} \equiv$$
 rate of tech progress

•  $e_t \equiv$  average quality

$$\psi'(e_t) > 0; \quad \psi''(e_t) < 0; \quad \psi(0) = 0$$

• The average quality of the population has a positive and diminishing effect on technological progress

Т	heory	

# Technological Progress



The	e Mair	n Elements

# Origins of Human Capital Formation

Theory

• The increase in the rate of technological progress increases the demand for human capital

# Origins of Human Capital Formation

Theory

- The increase in the rate of technological progress increases the demand for human capital
  - Human capital permits individuals to better cope with the changes in the technological environment

# Origins of Human Capital Formation

Theory

- The increase in the rate of technological progress increases the demand for human capital
  - Human capital permits individuals to better cope with the changes in the technological environment
  - The introduction of new technologies is skill-biased in the short-run, although the nature of the technology can be skill-biased or skill-saving in the long run

# Human Capital Formation

#### Human capital of an individual who joins the labor force in period t+1

$$h_{t+1} = h(e_{t+1}, g_{t+1})$$

# Human Capital Formation

Human capital of an individual who joins the labor force in period t+1

$$h_{t+1} = h(e_{t+1}, g_{t+1})$$

•  $e_{t+1} \equiv$  the individual education level (determined by parental investment, subject to their subsistence constraint, in period t)

Human capital of an individual who joins the labor force in period t+1

$$h_{t+1} = h(e_{t+1}, g_{t+1})$$

- $e_{t+1} \equiv$  the individual education level (determined by parental investment, subject to their subsistence constraint, in period t)
- $g_{t+1} \equiv$  rate of tech progress

#### The Main Elements

# Human Capital Formation

$$h_{t+1} = h(e_{t+1}, g_{t+1})$$

• 
$$h_e(e,g) > 0$$
 and  $h_{ee}(e,g) < 0$ 

• HC is increasing (in decreasing rates) in the parental time investment in the education of the child

#### The Main Elements

## Human Capital Formation

$$h_{t+1} = h(e_{t+1}, g_{t+1})$$

•  $h_e(e,g) > 0$  and  $h_{ee}(e,g) < 0$ 

- HC is increasing (in decreasing rates) in the parental time investment in the education of the child
- $h_g(e,g) < 0$  and  $h_{gg}(e,g) > 0$ 
  - Obsolescence of HC in a changing technological environment

#### The Main Elements

# Human Capital Formation

$$h_{t+1} = h(e_{t+1}, g_{t+1})$$

•  $h_e(e,g) > 0$  and  $h_{ee}(e,g) < 0$ 

• HC is increasing (in decreasing rates) in the parental time investment in the education of the child

• 
$$h_g(e,g) < 0$$
 and  $h_{gg}(e,g) > 0$ 

- Obsolescence of HC in a changing technological environment
- $h_{eg}(e,g) > 0$ 
  - Education lessens the obsolescence of HC in a changing technological environment
#### The Main Elements

## Human Capital Formation

$$h_{t+1} = h(e_{t+1}, g_{t+1})$$

•  $h_e(e,g) > 0$  and  $h_{ee}(e,g) < 0$ 

• HC is increasing (in decreasing rates) in the parental time investment in the education of the child

• 
$$h_g(e,g) < 0$$
 and  $h_{gg}(e,g) > 0$ 

- Obsolescence of HC in a changing technological environment
- $h_{eg}(e,g) > 0$ 
  - Education lessens the obsolescence of HC in a changing technological environment
- h(0,g) > 0
  - Basic level of human capital

# Human Capital Formation



#### The Main Elements

# Human Capital Formation



_		
	hoong	
	neorv	

• The rise in the demand for human capital induces parents to substitute quality for quantity of children

- The rise in the demand for human capital induces parents to substitute quality for quantity of children
- The rise in income along with the rise in the potential return to human capital generates:

- The rise in the demand for human capital induces parents to substitute quality for quantity of children
- The rise in income along with the rise in the potential return to human capital generates:
  - An income effect more income to spend on children

- The rise in the demand for human capital induces parents to substitute quality for quantity of children
- The rise in income along with the rise in the potential return to human capital generates:
  - An income effect more income to spend on children
  - Substitution effects

- The rise in the demand for human capital induces parents to substitute quality for quantity of children
- The rise in income along with the rise in the potential return to human capital generates:
  - An income effect more income to spend on children
  - Substitution effects
    - The opportunity cost of raising children increases

- The rise in the demand for human capital induces parents to substitute quality for quantity of children
- The rise in income along with the rise in the potential return to human capital generates:
  - An income effect more income to spend on children
  - Substitution effects
    - The opportunity cost of raising children increases
    - Return to investment in child quality increases

т	heony	
	neory	

• Early part of the second phase of industrialization:

_		
	hoong	
	neorv	

- Early part of the second phase of industrialization:
  - The income effect dominates (moderate demand for human capital):

- Early part of the second phase of industrialization:
  - The income effect dominates (moderate demand for human capital):
    - Population growth & human capital formation increase:

- Early part of the second phase of industrialization:
  - The income effect dominates (moderate demand for human capital):
    - Population growth & human capital formation increase:
- Later part of the second phase of industrialization:

- Early part of the second phase of industrialization:
  - The income effect dominates (moderate demand for human capital):
    - Population growth & human capital formation increase:
- Later part of the second phase of industrialization:
  - The substitution effect dominates (significant demand for human capital):

- Early part of the second phase of industrialization:
  - The income effect dominates (moderate demand for human capital):
    - Population growth & human capital formation increase:
- Later part of the second phase of industrialization:
  - The substitution effect dominates (significant demand for human capital):
    - Population growth declines & human capital formation increases further

Theory	Individuals	
Individuals		

• Live for 2 periods

Theory	Individuals	
Individuals		

- Live for 2 periods
- Childhood (1st Period):

Theory	Individuals	
Individuals		

- Live for 2 periods
- Childhood (1st Period):
  - Consume a fraction of parental time endowment

Theory	Individuals	
Individuals		

- Live for 2 periods
- Childhood (1st Period):
  - Consume a fraction of parental time endowment
  - The required time increases with child quality

Theory	Individuals	
Individuals		

- Live for 2 periods
- Childhood (1st Period):
  - Consume a fraction of parental time endowment
  - The required time increases with child quality
    - $\tau \equiv \text{ time required to raise a child, regardless of quality}$

Theory	Individuals	
Individuals		

- Live for 2 periods
- Childhood (1st Period):
  - Consume a fraction of parental time endowment
  - The required time increases with child quality
    - $\tau \equiv \text{ time required to raise a child, regardless of quality}$
    - $au + e_{t+1} \equiv$  time to raise a child with education  $e_{t+1}$

Theory	Individuals	
Individuals		

- Live for 2 periods
- Childhood (1st Period):
  - Consume a fraction of parental time endowment
  - The required time increases with child quality
    - $\tau \equiv \text{ time required to raise a child, regardless of quality}$
    - $au + e_{t+1} \equiv$  time to raise a child with education  $e_{t+1}$
- Parenthood (2nd Period):

Theory	Individuals	
Individuals		

- Live for 2 periods
- Childhood (1st Period):
  - Consume a fraction of parental time endowment
  - The required time increases with child quality
    - $\tau \equiv \text{ time required to raise a child, regardless of quality}$
    - $au + e_{t+1} \equiv$  time to raise a child with education  $e_{t+1}$
- Parenthood (2nd Period):
  - Allocate the time endowment between childrearing and work

Theory	Individuals	
Individuals		

- Live for 2 periods
- Childhood (1st Period):
  - Consume a fraction of parental time endowment
  - The required time increases with child quality
    - $\tau \equiv \text{ time required to raise a child, regardless of quality}$
    - $au + e_{t+1} \equiv$  time to raise a child with education  $e_{t+1}$
- Parenthood (2nd Period):
  - Allocate the time endowment between childrearing and work
  - Choose the optimal mixture of child quantity and quality

Theory	Individuals	
Individuals		

- Live for 2 periods
- Childhood (1st Period):
  - Consume a fraction of parental time endowment
  - The required time increases with child quality
    - $\tau \equiv \text{ time required to raise a child, regardless of quality}$
    - $au + e_{t+1} \equiv$  time to raise a child with education  $e_{t+1}$
- Parenthood (2nd Period):
  - Allocate the time endowment between childrearing and work
  - Choose the optimal mixture of child quantity and quality
  - Consume

Individuals

## The Darwinian Elements

- Variety
  - Preferences for child quality differ across individuals

Individuals

#### The Darwinian Elements

- Variety
  - Preferences for child quality differ across individuals
  - Quality type & Quantity type
- Natural selection
  - Evolutionary advantage for types with the highest reproduction success

Individuals

#### The Darwinian Elements

- Variety
  - Preferences for child quality differ across individuals
  - Quality type & Quantity type
- Natural selection
  - Evolutionary advantage for types with the highest reproduction success
- Evolution
  - Changes in the composition of types

Theory	Individuals	
Preferences		

$$u_t^i = (1 - \gamma) \ln c_t^i + \gamma [\ln n_t^i + eta^i \ln h_{t+1}^i]$$

Theory	Individuals	
Preferences		

$$u_t^i = (1-\gamma) \ln c_t^i + \gamma [\ln n_t^i + eta^i \ln h_{t+1}^i]$$

•  $c_t^i \equiv$  consumption of individual of type *i* in generation *t* 

Theory	Individuals	
Preferences		

$$u_t^i = (1-\gamma) \ln c_t^i + \gamma [\ln n_t^i + eta^i \ln h_{t+1}^i]$$

•  $c_t^i \equiv$  consumption of individual of type *i* in generation *t* •  $n_t^i \equiv$  number of children of individual of type *i* in generation *t* 

Theory	Individuals	
Preferences		

$$u_t^i = (1 - \gamma) \ln c_t^i + \gamma [\ln n_t^i + eta^i \ln h_{t+1}^i]$$

cⁱ_t ≡ consumption of individual of type i in generation t
nⁱ_t ≡ number of children of individual of type i in generation t
hⁱ_{t+1} ≡ human capital of each child of member i of generation t

Theory	Individuals	
Preferences		

$$u_t^i = (1 - \gamma) \ln c_t^i + \gamma [\ln n_t^i + eta^i \ln h_{t+1}^i]$$

•  $c_t^i \equiv$  consumption of individual of type *i* in generation *t* •  $n_t^i \equiv$  number of children of individual of type *i* in generation *t* •  $h_{t+1}^i \equiv$  human capital of each child of member *i* of generation *t* •  $\beta^i \equiv$  predisposition towards quality of individual of type *i* 

Theory	Individuals	
Preferences		

$$u_t^i = (1 - \gamma) \ln c_t^i + \gamma [\ln n_t^i + eta^i \ln h_{t+1}^i]$$

- cⁱ_t ≡ consumption of individual of type *i* in generation *t*nⁱ_t ≡ number of children of individual of type *i* in generation *t*hⁱ_{t+1} ≡ human capital of each child of member *i* of generation *t*βⁱ ≡ predisposition towards quality of individual of type *i*
- Intergenerational transmission of predisposition towards quality

$$eta^i_{t+1}=eta^i_t=eta^i$$

Theory	Individuals	
Preferences		

- Preferences reflect the implicit Darwinian survival strategy.
  - Individuals do not operate consciously so as to assure the evolutionary advantage of their type (i.e., their variant within the species)

I heory	Individuals	
Preferences		

- Preferences reflect the implicit Darwinian survival strategy.
  - Individuals do not operate consciously so as to assure the evolutionary advantage of their type (i.e., their variant within the species)
    - The existence of variety of types enables nature to select those who fit the economic environment
| I heory     | Individuals |  |
|-------------|-------------|--|
| Preferences |             |  |
|             |             |  |

- Preferences reflect the implicit Darwinian survival strategy.
  - Individuals do not operate consciously so as to assure the evolutionary advantage of their type (i.e., their variant within the species)
    - The existence of variety of types enables nature to select those who fit the economic environment
  - Capture the most fundamental trade-offs in nature:

I heory	Individuals	
Preferences		

- Preferences reflect the implicit Darwinian survival strategy.
  - Individuals do not operate consciously so as to assure the evolutionary advantage of their type (i.e., their variant within the species)
    - The existence of variety of types enables nature to select those who fit the economic environment
  - Capture the most fundamental trade-offs in nature:
    - Resources allocated to the parent vs. offspring

I heory	Individuals	
Preferences		

- Preferences reflect the implicit Darwinian survival strategy.
  - Individuals do not operate consciously so as to assure the evolutionary advantage of their type (i.e., their variant within the species)
    - The existence of variety of types enables nature to select those who fit the economic environment
  - Capture the most fundamental trade-offs in nature:
    - Resources allocated to the parent vs. offspring
    - Resources allocated to the number vs. quality of offspring

I heory	Individuals	
Preferences		

- Preferences reflect the implicit Darwinian survival strategy.
  - Individuals do not operate consciously so as to assure the evolutionary advantage of their type (i.e., their variant within the species)
    - The existence of variety of types enables nature to select those who fit the economic environment
  - Capture the most fundamental trade-offs in nature:
    - Resources allocated to the parent vs. offspring
    - Resources allocated to the number vs. quality of offspring
    - Consumption above subsistence assure that survival of the parent & lineage

Individuals

### Budget and Subsistence Consumption Constraints

$$w_t h_t^i n_t^i (\tau + e_{t+1}^i) + c_t^i \le w_t h_t^i \equiv z_t^i$$

- $z_t^i \equiv$  potential income of individual t
- $au \equiv$  time required to raise a child, regardless of quality
- $au + e^i_{t+1} \equiv$  time needed to raise a child with education  $e^i_{t+1}$

Individuals

### Budget and Subsistence Consumption Constraints

$$w_t h_t^i n_t^i (\tau + e_{t+1}^i) + c_t^i \le w_t h_t^i \equiv z_t^i$$

- $z_t^i \equiv$  potential income of individual t
- $au \equiv$  time required to raise a child, regardless of quality
- $au + e^i_{t+1} \equiv$  time needed to raise a child with education  $e^i_{t+1}$
- Subsistence consumption constraint:

$$c_t \geq \tilde{c}$$

Individuals

# Constraint and Optimization



Theory
--------

Individuals

# Optimal Investment in Child Quality of the Qantity type



Т	heorv	

Individuals

# Optimal Investment in Child Quality of the Quality type



Individuals

## Optimal Investment in Child Quality - Quality type - and Qantity type



Individuals

## **Optimization – Malthusian Epoch**



65 / 75

Individuals

## Evolutionary Advantage of the Quality Type



Individuals

## Differential Fertlity Across Types



## The Dynamical System

A sequence  $\{x_t, g_t, e_t, q_t\}_{t=0}^\infty$  such that:

$$egin{aligned} & (x_{t+1} = x(g_t, x_t, q_t)) \ & q_{t+1} = q(g_t, x_t, q_t) \ & g_{t+1} = \psi(e_t) \ & e_t = e(g_t, q_t) \end{aligned}$$

The Conditional Evolution of Technology and Education

 $\{g_t, e_t; q\}_{t=0}^\infty$  such that for all t

$$\begin{cases} e_t = e(g_t; q) \\ g_{t+1} = \psi(e_t). \end{cases}$$

_		
	hoong	
	neurv	

# **Technological Progress**



Т	h	e	0	r٧	

#### The Dynamical System

# **Technological Progress**



Theory	The Dynamical System	

The Evolution of Education and Technology: The Fraction of the Quality Type  $q{=}0$ 



The Dynamical Syste
---------------------

The Evolution of Education and Technology: The Fraction of the Quality Type  $q\!>\!0$ 



Theory

Т	heory	

The Evolution of Education and Technology: The Fraction of the Quality Type is Above the Threshold



-		
	neorv	

# The Evolution of the Quality Type and TFP Growth

